

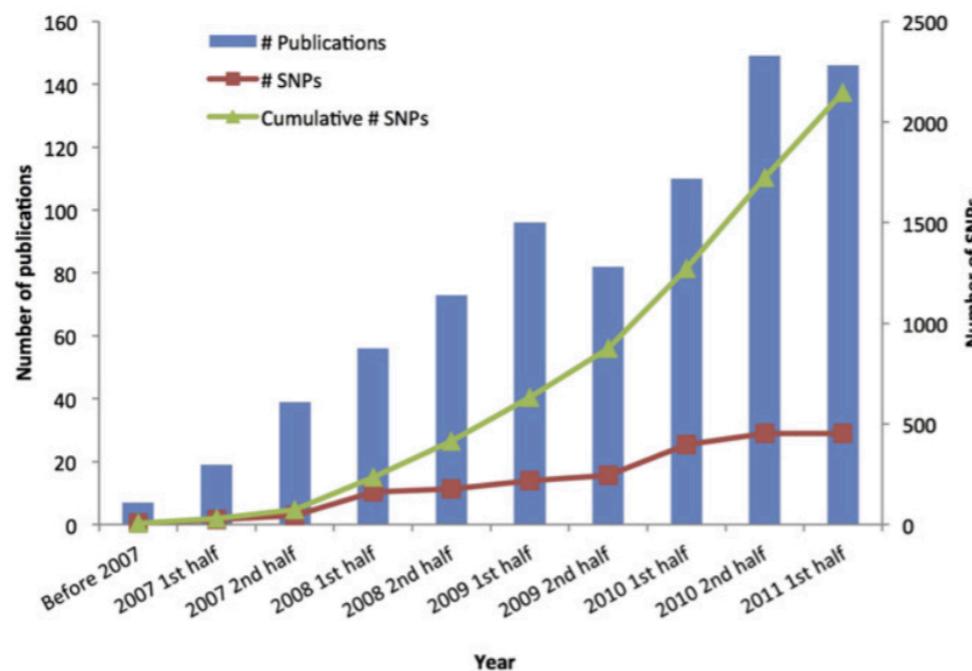
Machine Learning for large-scale genomics

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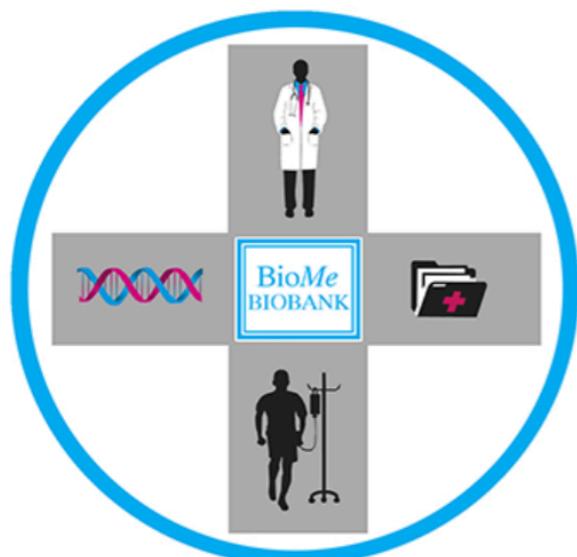
Genetic architecture of complex phenotypes

$$\text{Phenotype} = f(\text{Genotype}, \text{Environment})$$



Visscher et al. AJHG 2012

Growth of Biobanks



BIOVU



Machine Learning for Biobank-scale data

How can we learn about genetic architecture
of complex traits and diseases from datasets
that contain millions of genomes and
thousands of traits ?

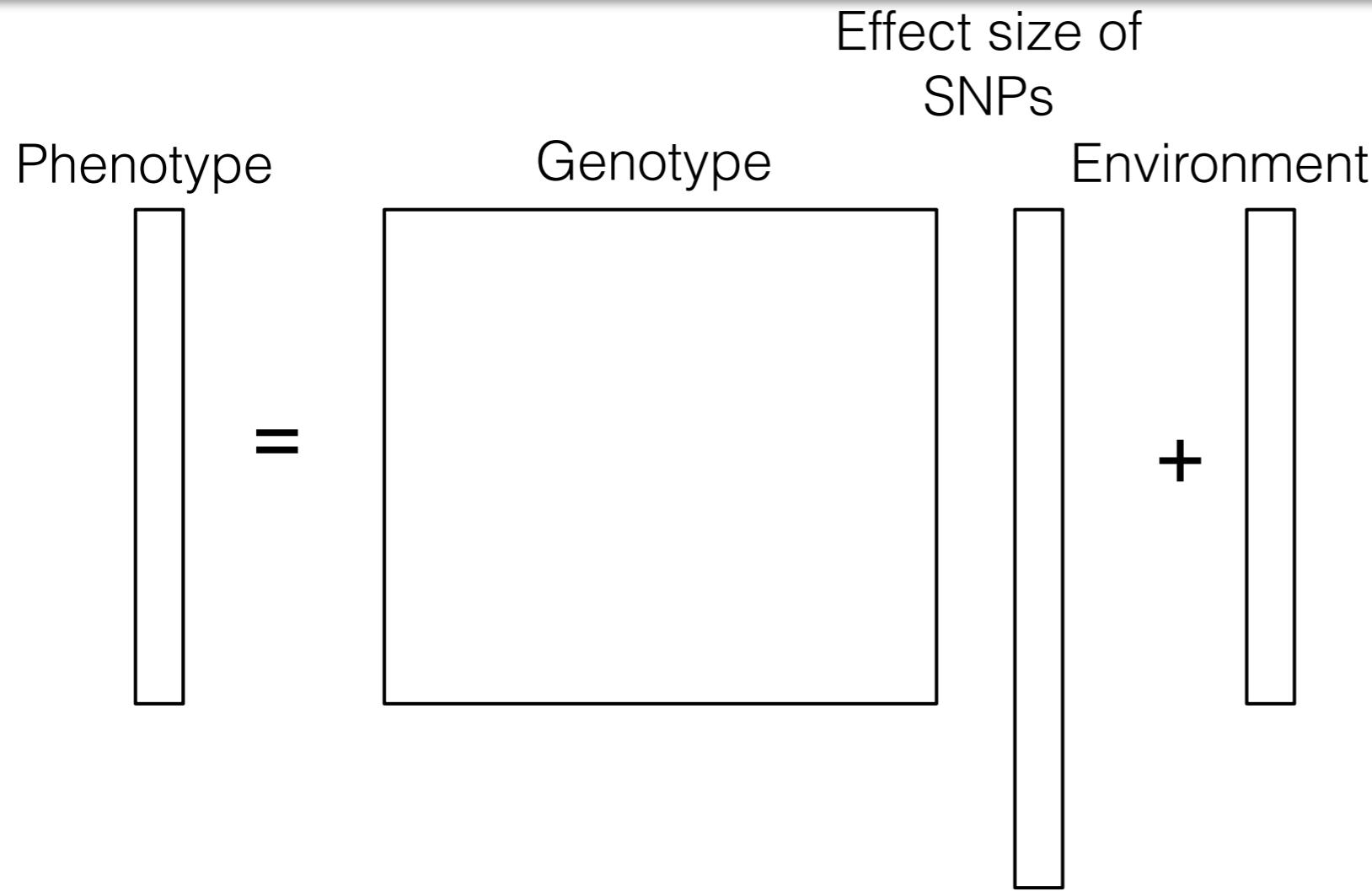
Statistical

Privacy

Computational

Interpretability

(Narrow-sense) Heritability



$$h^2 = \frac{\sigma_g^2}{\sigma_g^2 + \sigma_e^2}$$

SNP heritability

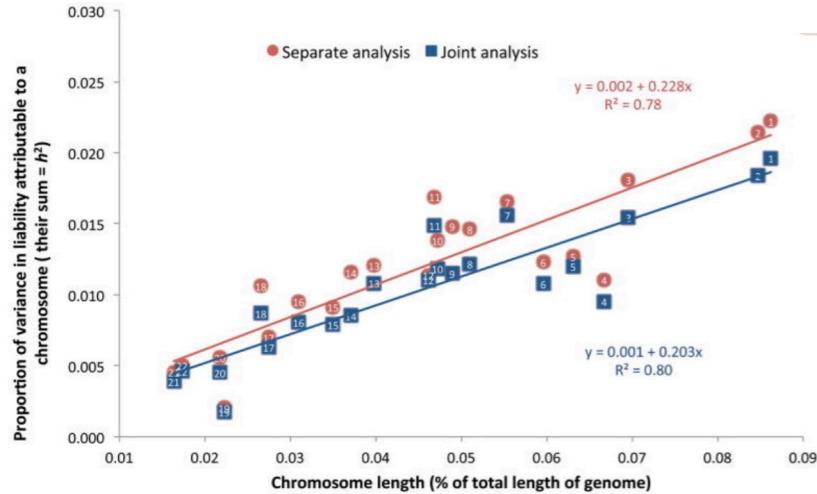
$$Y = X \beta + \epsilon$$

$$\beta_m \sim \mathcal{N}(0, \frac{\sigma_g^2}{M}) \quad \epsilon_n \sim \mathcal{N}(0, \sigma_e^2)$$

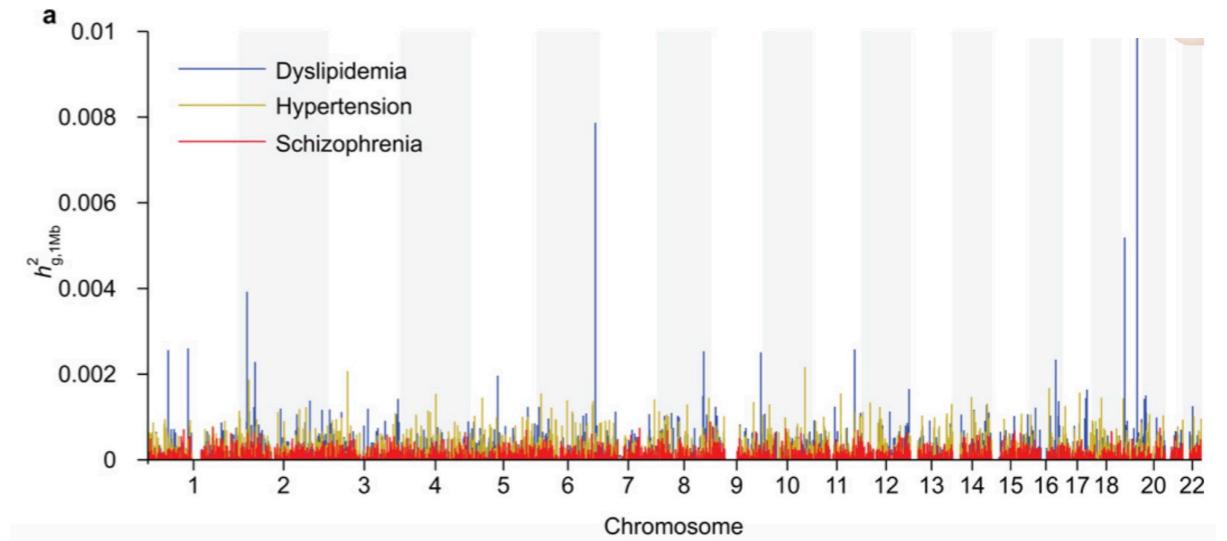
Environmental variance
component

Genetic variance component

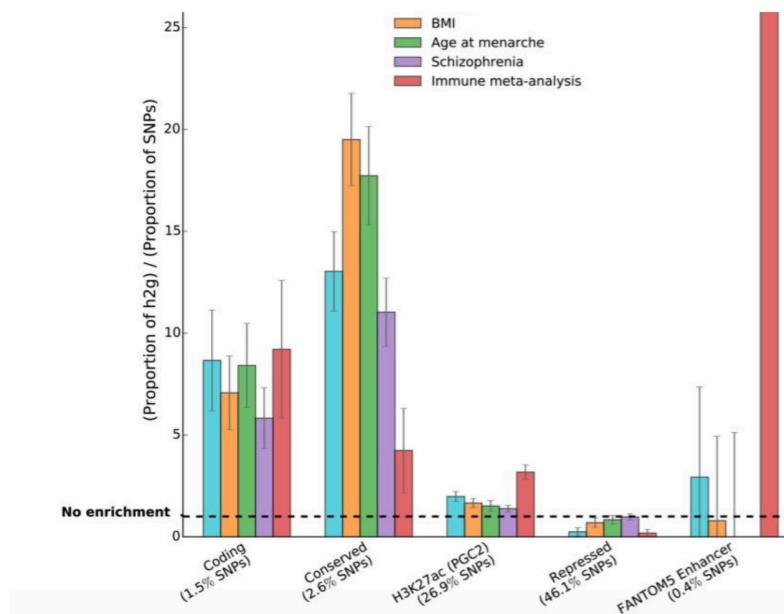
Beyond Heritability



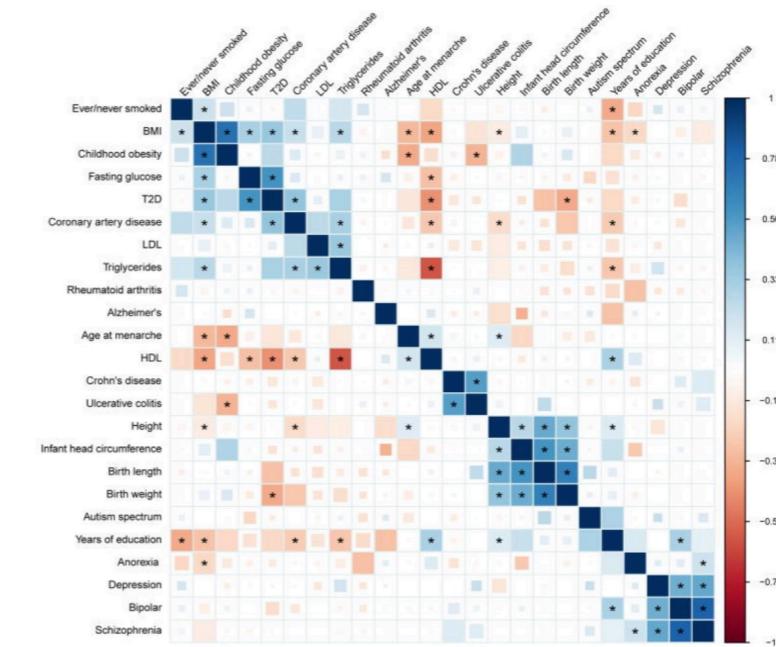
Lee et al. 2012



Loh et al. 2015



Finucane et al. 2015



Bulk-Sullivan et al. 2015

Variance components model

$$\mathbf{y} = \sum_{k=1}^K \mathbf{X}_k \boldsymbol{\beta}_k + \boldsymbol{\epsilon}$$

$$\boldsymbol{\beta}_k \sim \mathcal{N}(\mathbf{0}, \frac{\sigma_k^2}{M_k} \mathbf{I}_{M_k}), k \in \{1, \dots, K\}$$

$$\boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0}, \sigma_e^2 \mathbf{I}_N)$$

Goal

Estimate variance components $(\sigma_1^2, \sigma_2^2, \dots, \sigma_K^2, \sigma_e^2)$

Estimating variance components

Maximum likelihood

$$\begin{aligned}(\hat{\sigma}_1^2, \hat{\sigma}_2^2, \dots, \hat{\sigma}_K^2, \hat{\sigma}_e^2) &= \operatorname{argmax}_{(\sigma_1^2, \dots, \sigma_K^2, \sigma_e^2)} \mathcal{LL}(\sigma_1^2, \dots, \sigma_K^2, \sigma_e^2) \\ &= \operatorname{argmax}_{(\sigma_1^2, \dots, \sigma_K^2, \sigma_e^2)} P(\mathbf{y} | \mathbf{X}_1, \dots, \mathbf{X}_K, \sigma_1^2, \dots, \sigma_K^2, \sigma_e^2)\end{aligned}$$

Computationally expensive

Scales as $\mathcal{O}(N^3)$

Challenging to apply to Biobank-scale data

Lippert et al. Nature Methods 2012
Zhou and Stephens, Nature Genetics 2012
Loh et al. Nature Genetics 2015

Randomized HE-regression (RHE-mc)

Combines randomization with a method-of-moments estimator

Work with a “sketch” of the genotype

Multiply the genotype matrix with B random vectors

Efficiency depends on B: $\mathcal{O}\left(\frac{MNB}{\log_3(\max(N, M))}\right)$

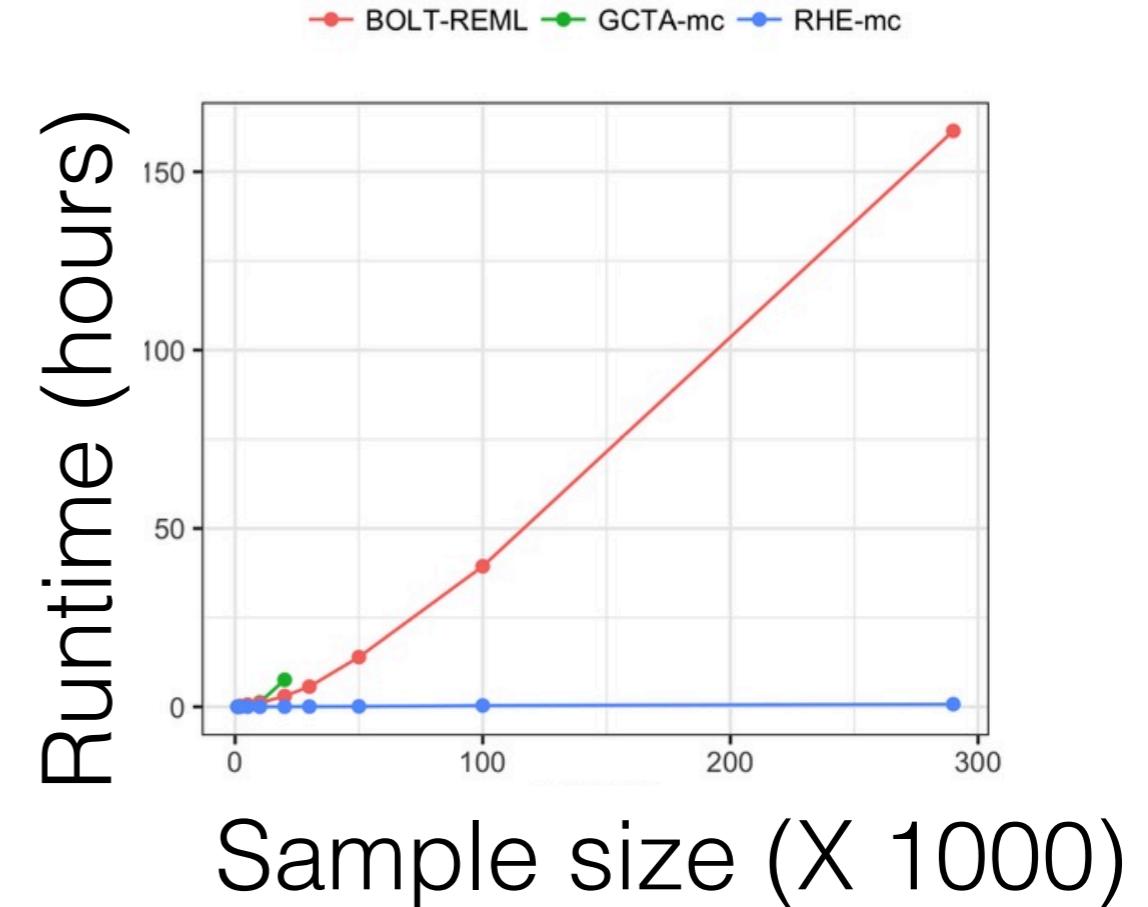
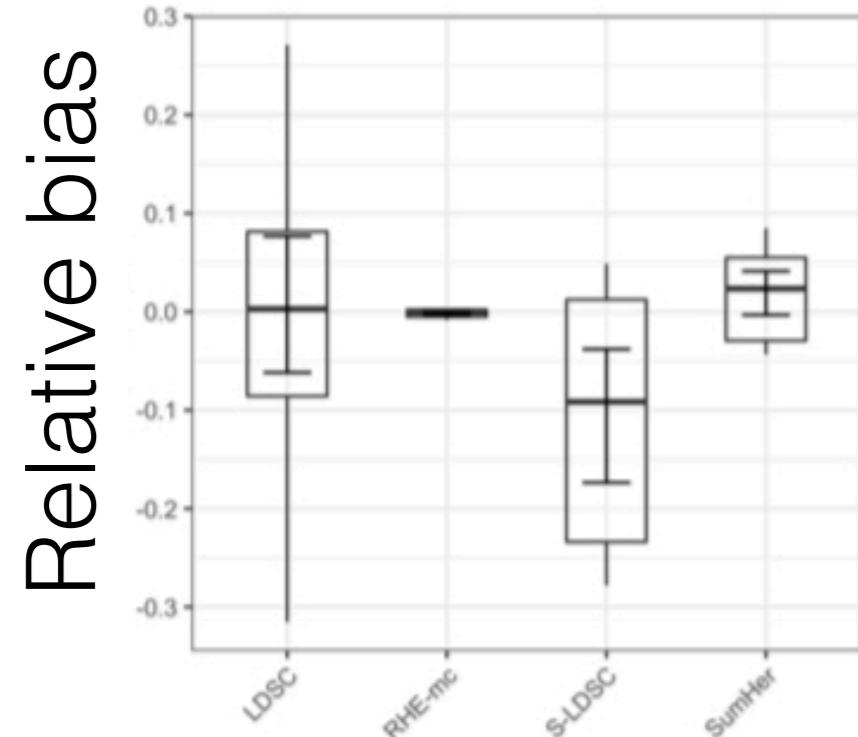
Accurate for B as small as 10

Hutchinson 1989

Wu et al. Bioinformatics 2018

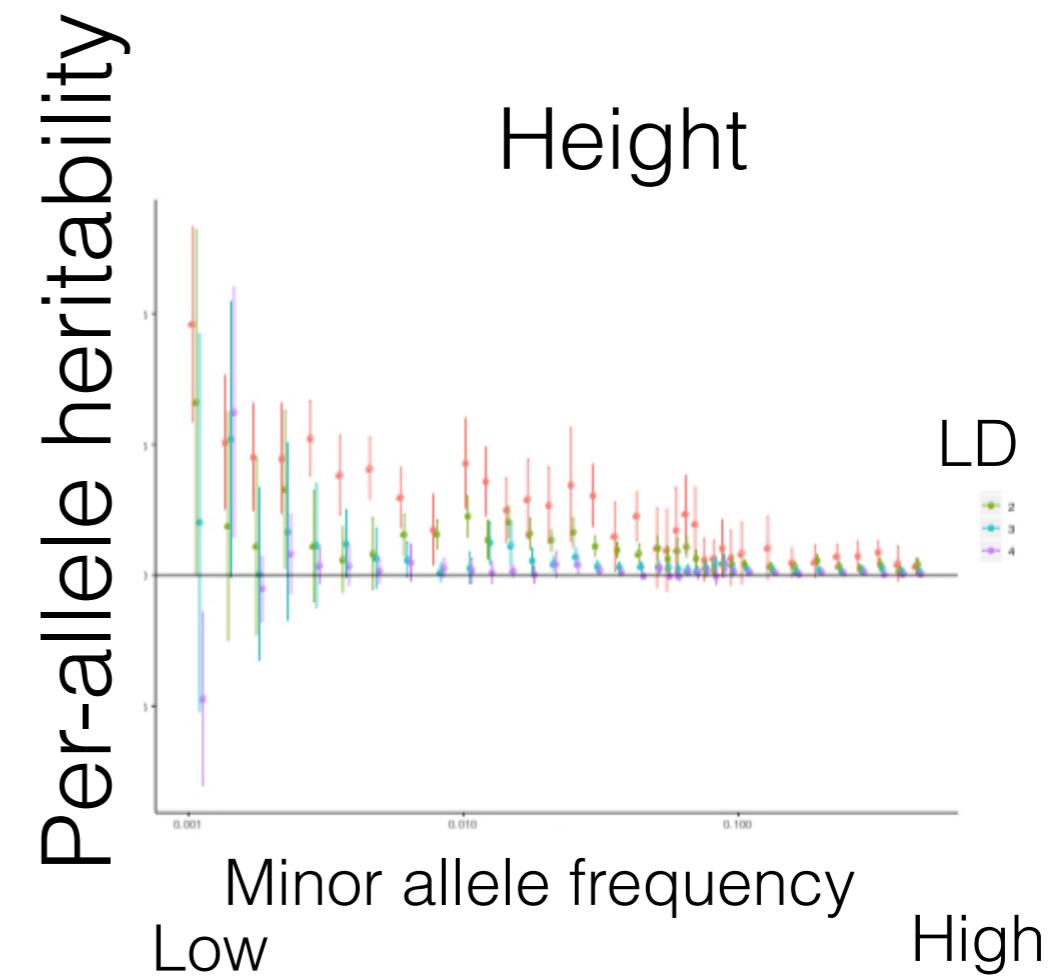
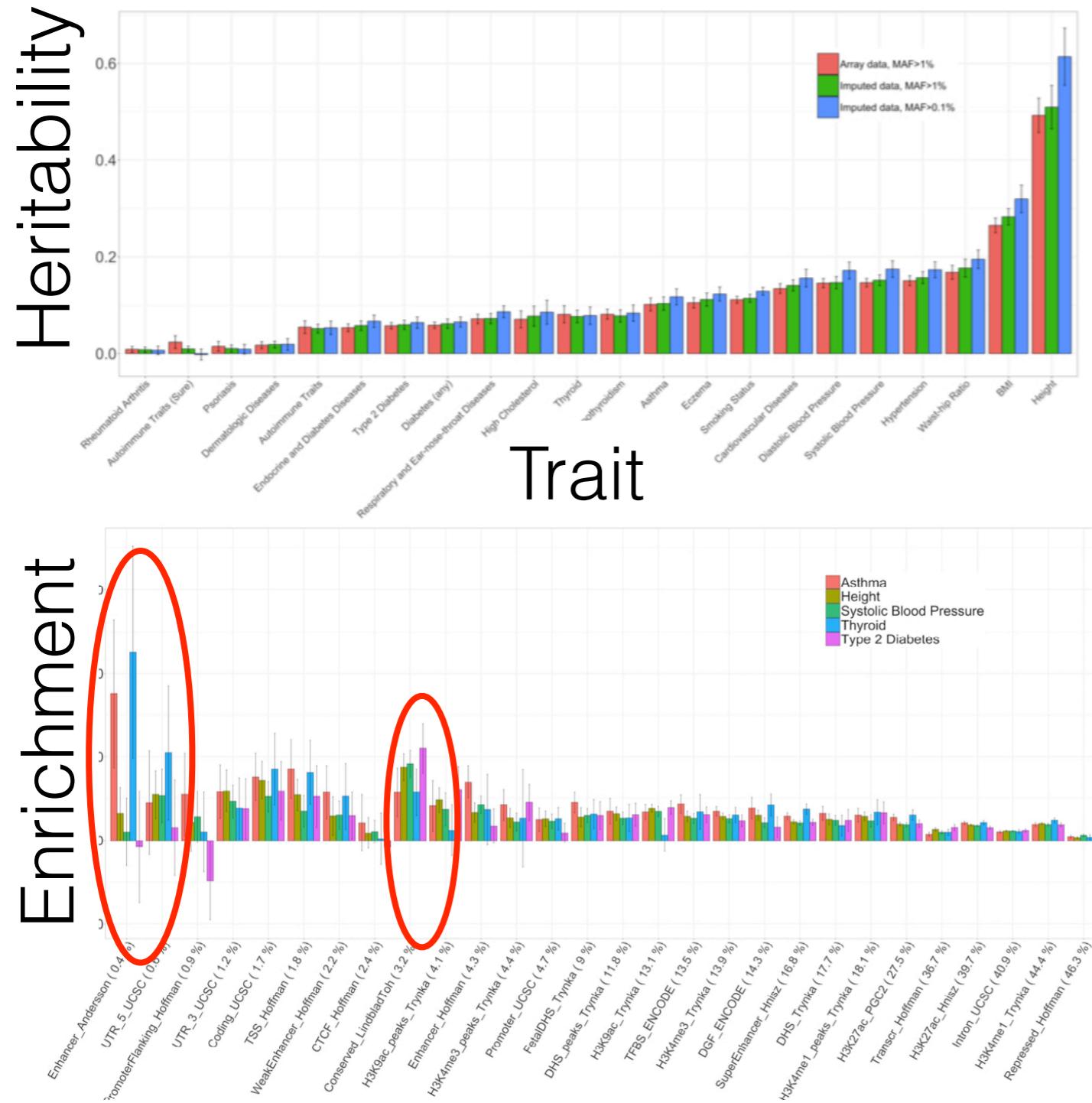
Pazokitoroudi et al. RECOMB 2019, Nature Communication 2020

Comparisons of RHE-mc



Pazokitoroudi et al. RECOMB 2019, Nature Communication 2020

Insights from Biobank-scale analysis



Pazokitoroudi et al. Nature Communication 2020

Beyond heritability

What is the contribution of non-linear effects ?

What is the contribution of environmental interactions ?

How are genetic effects shared across traits ?

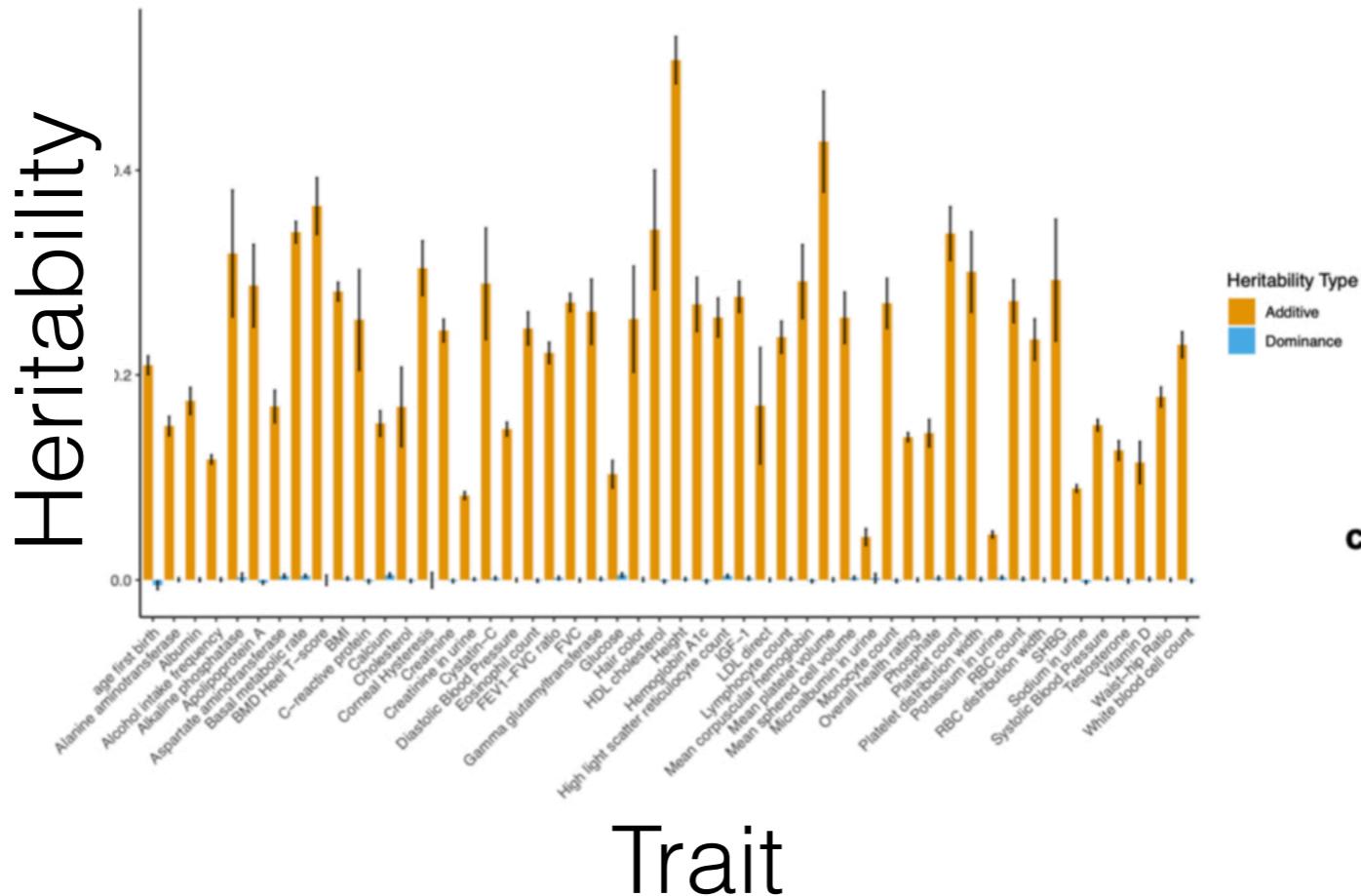
Dominance deviation effects

Additive variance component

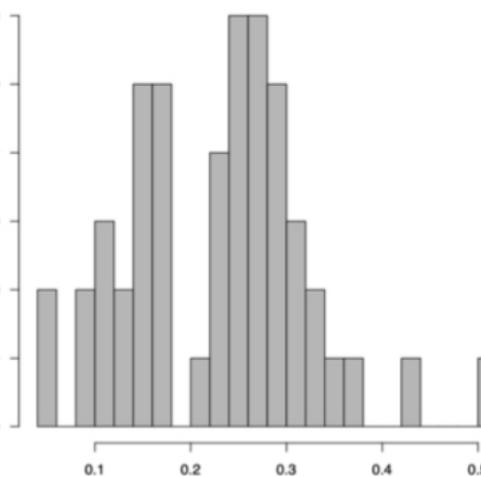
$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{D}\boldsymbol{\gamma} + \boldsymbol{\epsilon}$$

$$\boldsymbol{\beta} \sim \mathcal{N}(\mathbf{0}, \frac{\sigma_a^2}{M} \mathbf{I}_M)$$

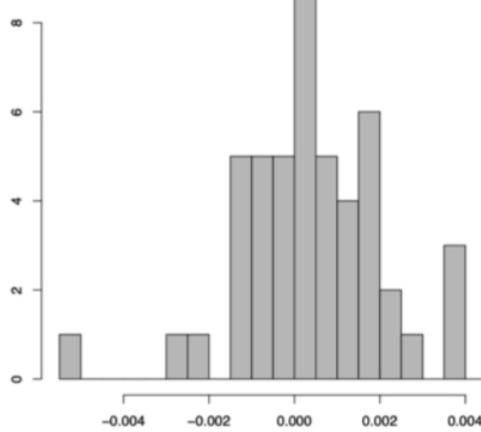
$$\boldsymbol{\gamma} \sim \mathcal{N}(\mathbf{0}, \frac{\sigma_d^2}{M} \mathbf{I}_M)$$



c



Additive heritability



Dominance heritability

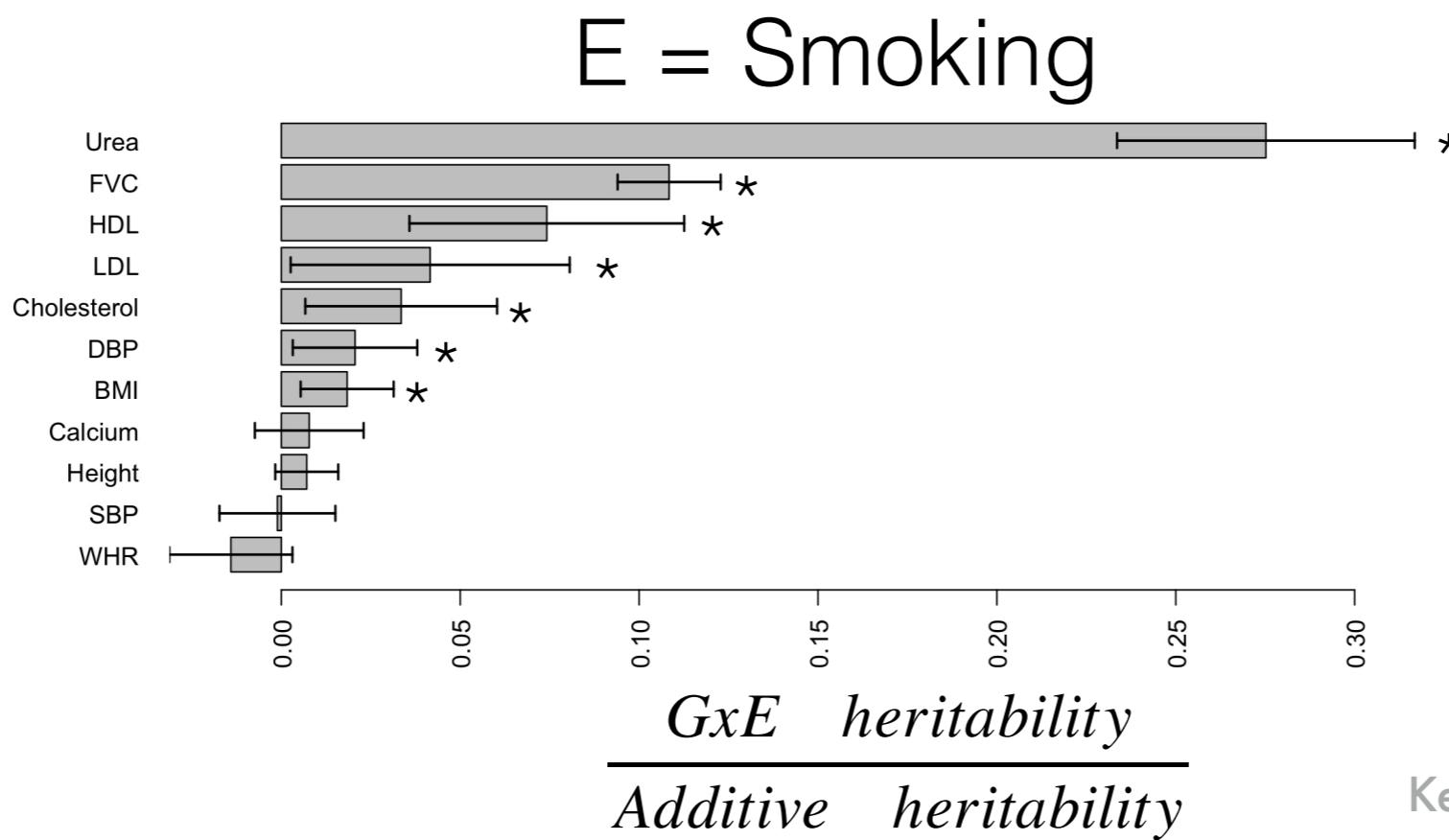
Hivert et al. AJHG (to appear)
Pazokitoroudi et al. AJHG (to appear)

Gene-environment interactions (GxE)

$$y = X\beta + X \odot E\delta + \epsilon$$

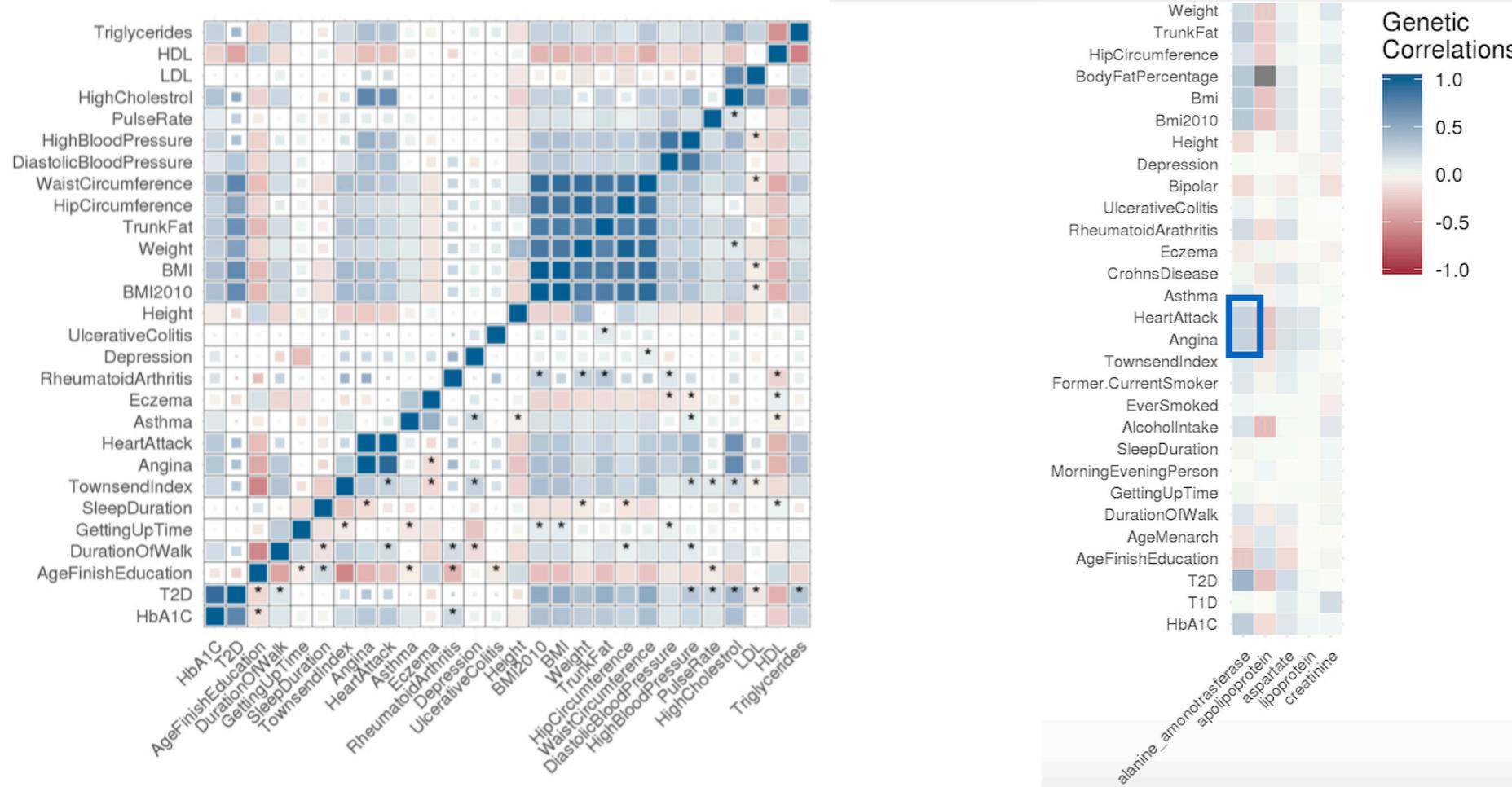
$$\delta \sim \mathcal{N}(0, \frac{\sigma_{GE}^2}{ML} I)$$

GxE variance component



Kerrin and Marchini AJHG 2020
Pazokitoroudi et al. RECOMB 2021

Genetic correlation



Novel genetic correlation of coronary artery disease and serum liver enzyme

Wu et al. RECOMB 2019, BioRxiv 2020



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Machine Learning and Genomics Lab

Scaling Machine Learning to Biobanks

Effectiveness of randomization

Approximate inference

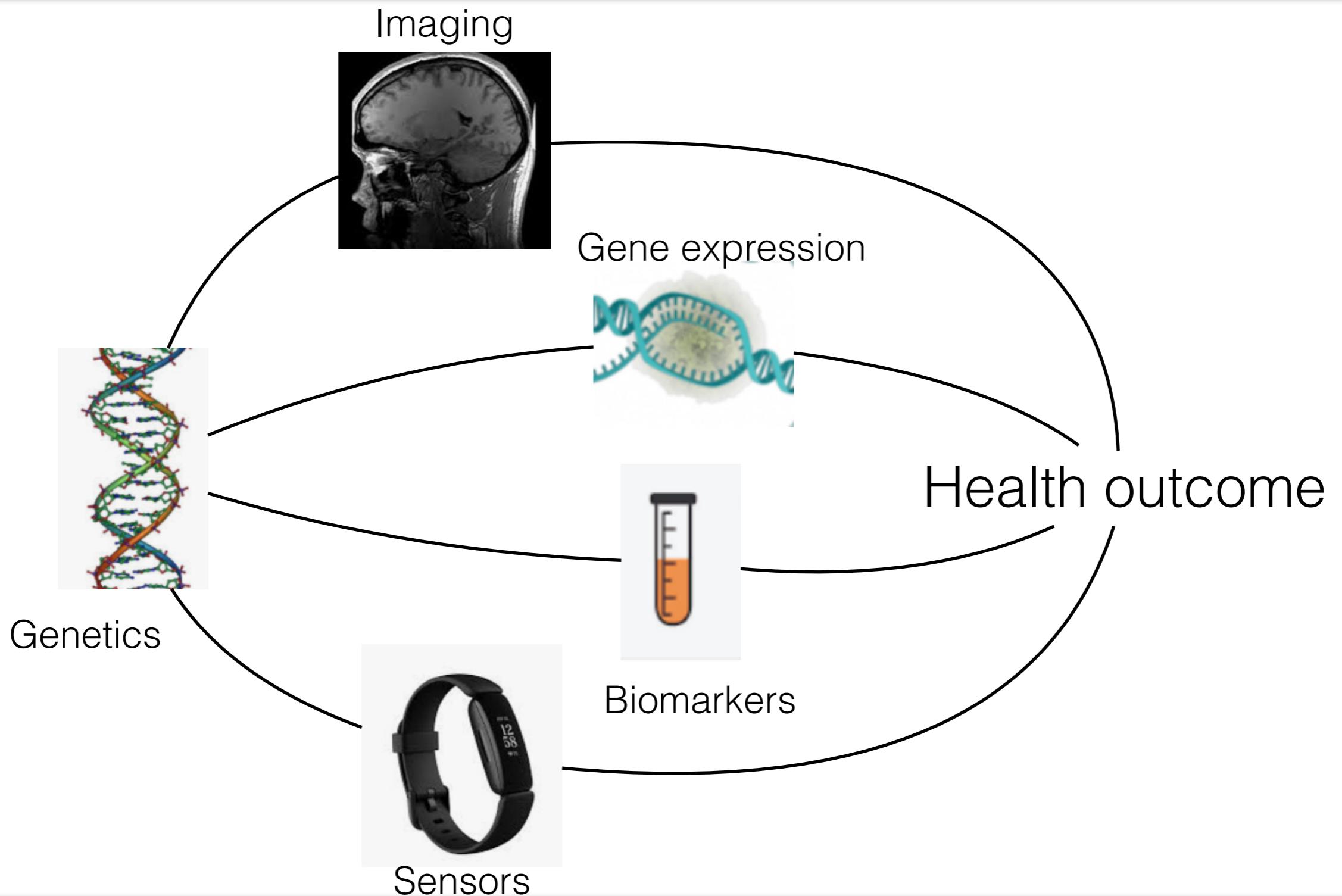
Distributed inference

Promises and challenges

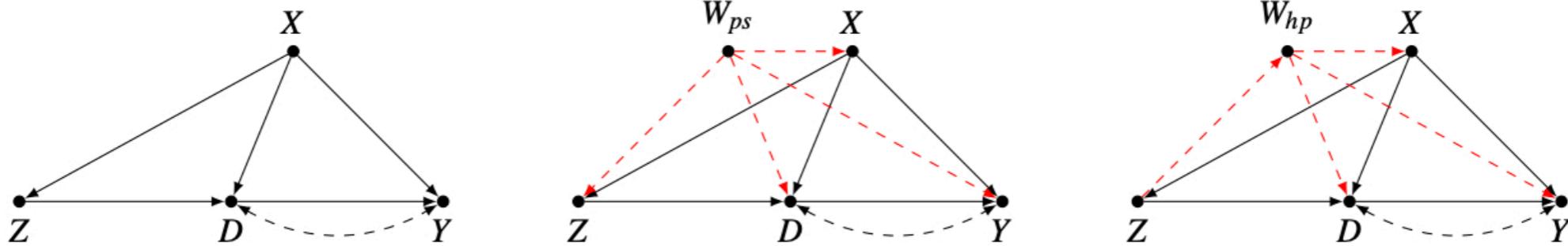
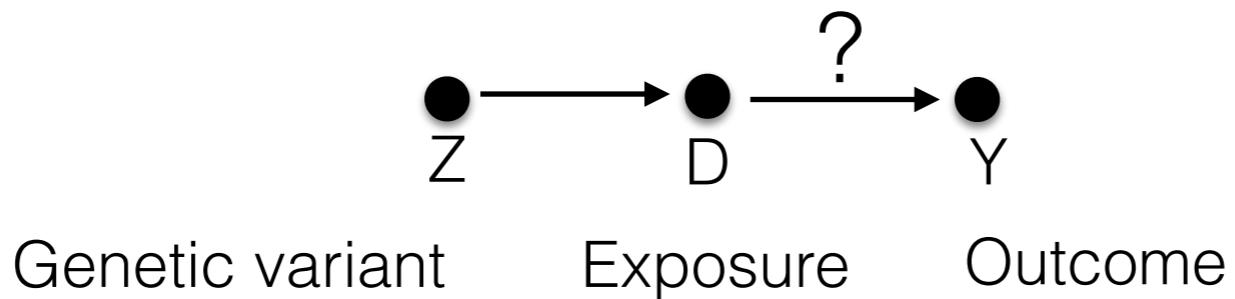


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Multi-modal data

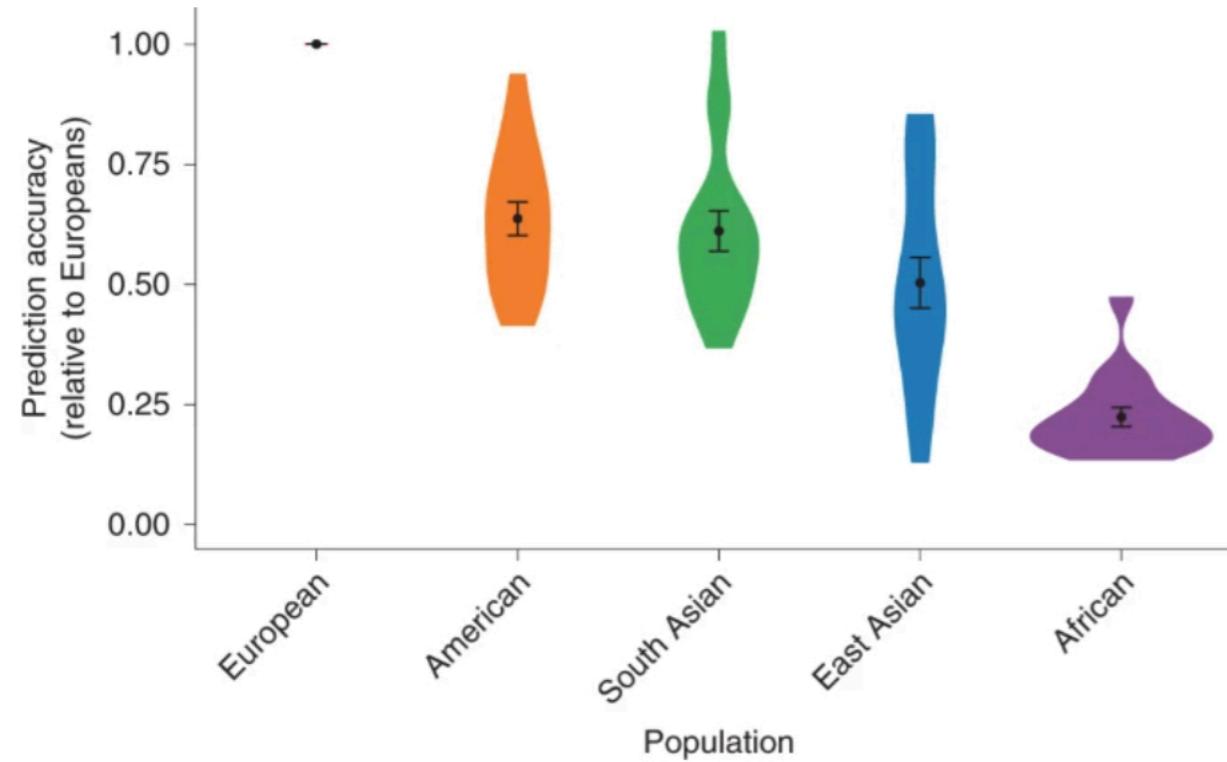


Causal inference



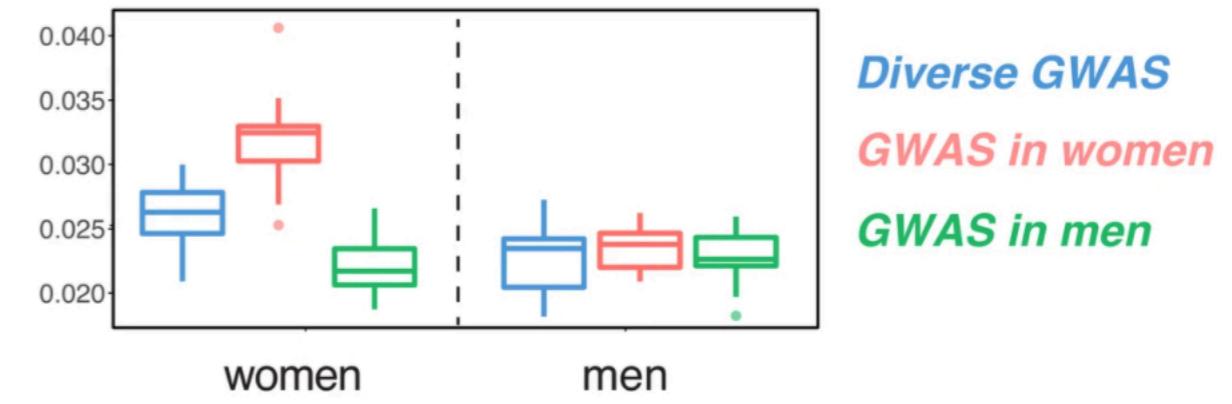
Katan et al. Lancet 1986
Brown et al. BioRxiv 2020
Cinelli et al. BioRxiv 2020

Generalizability



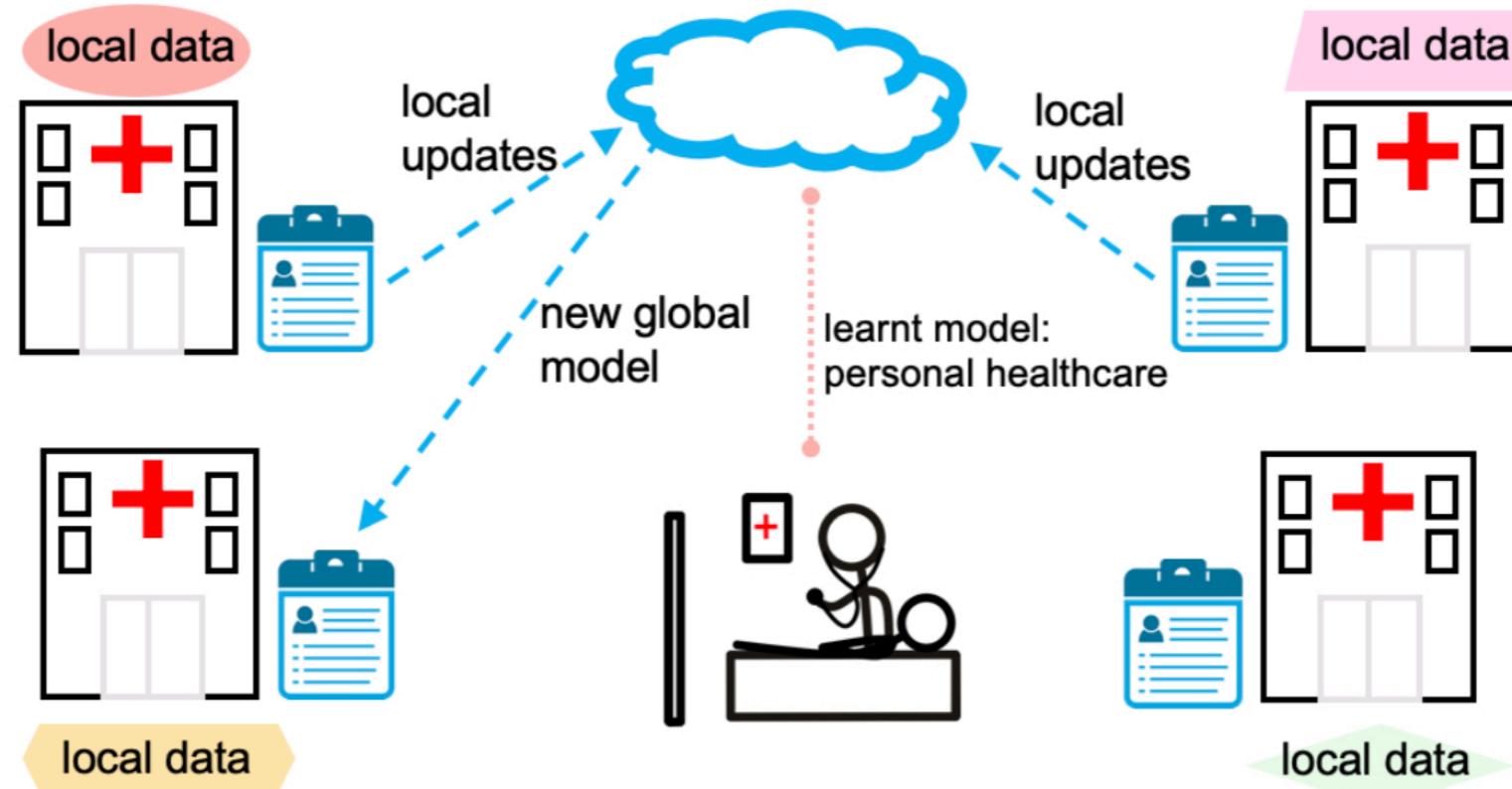
Martin et al. Nature Genetics 2019

A. Diastolic blood pressure



Mostafavi et al. eLife 2020

Distributed and federated ML



Acknowledgments



Funding

